

**CORTEX**

Core monitoring techniques and  
experimental validation and demonstration

# Combining simulations and machine learning for neutron noise-based core diagnostics

**IAEA Technical Meeting on Artificial Intelligence for Nuclear  
Technology and Applications  
October 25-29, 2021 – hybrid**

**On behalf of the CORTEX consortium:**

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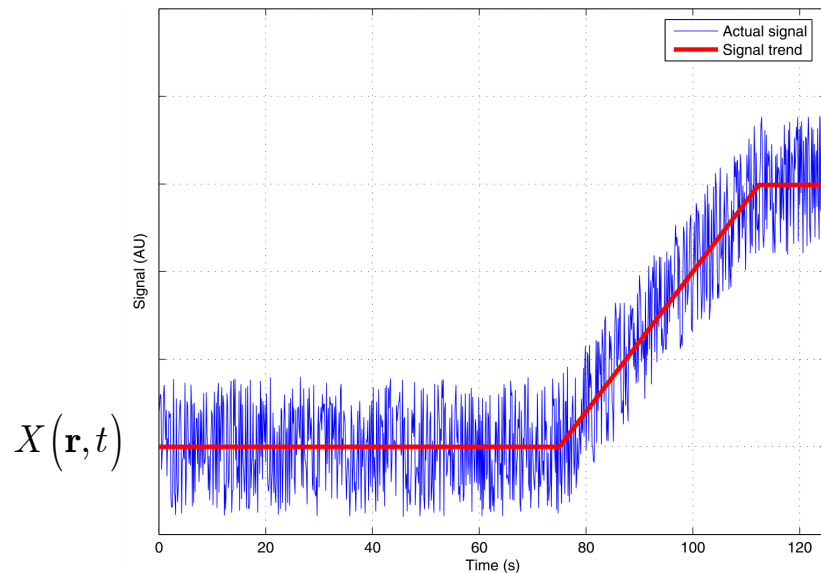
This project has received funding from the Euratom research and training programme 2014-2018 under grant agreement No 754316.

# Introduction and background



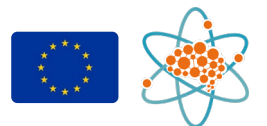
# Introduction and background

- Fluctuations always existing in dynamical systems even at steady state-conditions:



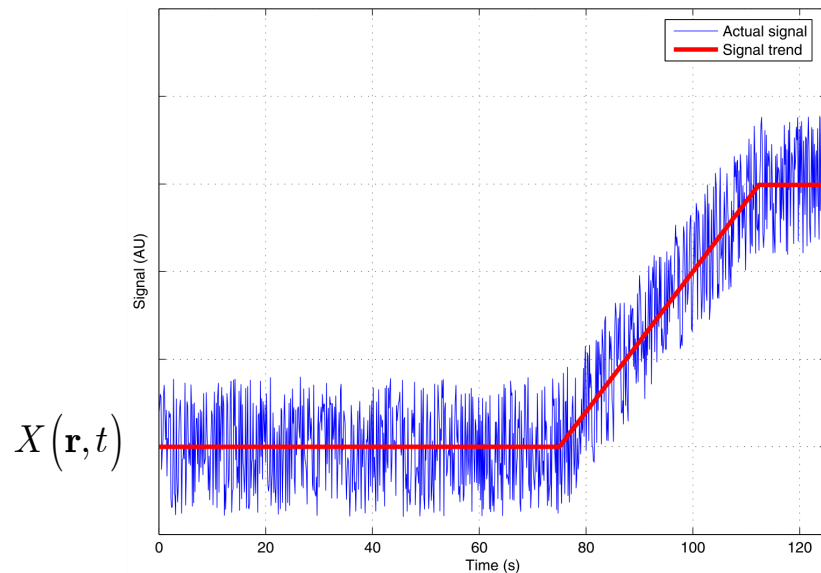
Conceptual illustration of the possible time-dependence of a measured signal from a dynamical system

$$X(\mathbf{r}, t) = X_0(\mathbf{r}, t) + \delta X(\mathbf{r}, t)$$



# Introduction and background

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Conceptual illustration of the possible time-dependence of a measured signal from a dynamical system

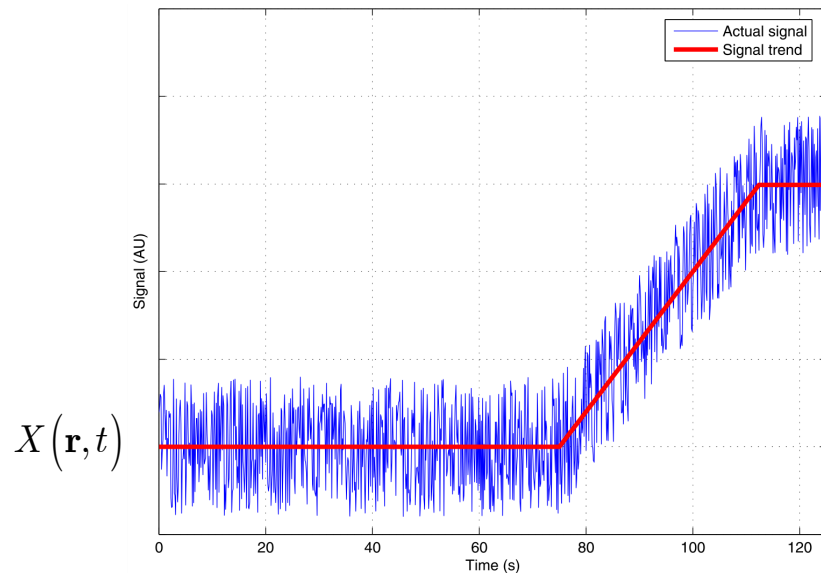
$$X(\mathbf{r}, t) = X_0(\mathbf{r}, t) + \delta X(\mathbf{r}, t)$$

actual  
signal



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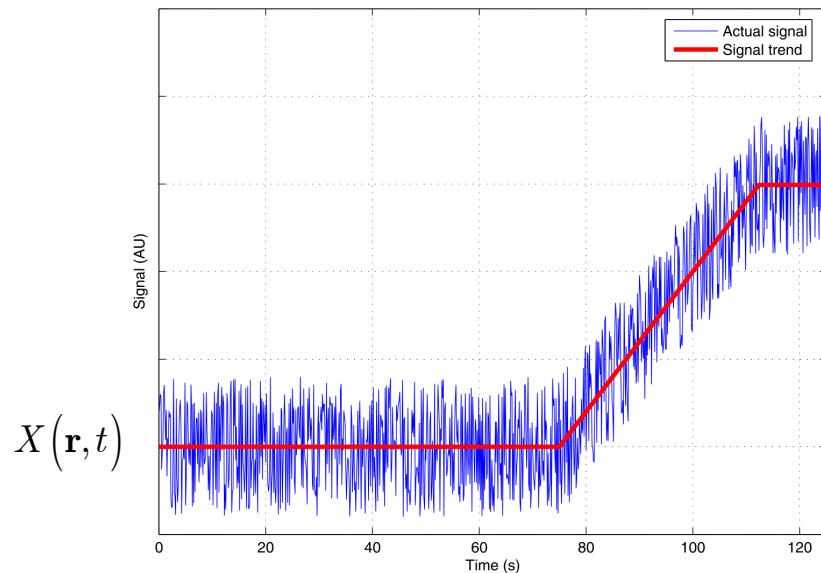
$$X(\mathbf{r}, t) = \underbrace{X_0(\mathbf{r}, t)}_{\text{signal}} + \delta X(\mathbf{r}, t)$$

trend or mean



# Introduction and background

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Conceptual illustration of the possible time-dependence of a measured signal from a dynamical system

$$X(\mathbf{r}, t) = X_0(\mathbf{r}, t) + \delta X(\mathbf{r}, t)$$

fluctuations  
or “noise”

- Fluctuations carrying some valuable information about the system dynamics



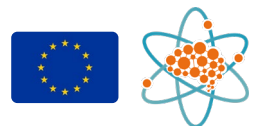
# Introduction and background

- Fluctuations could be used for “diagnostics”, i.e.:

- Early detection of anomalies
- Estimation of dynamical system characteristics

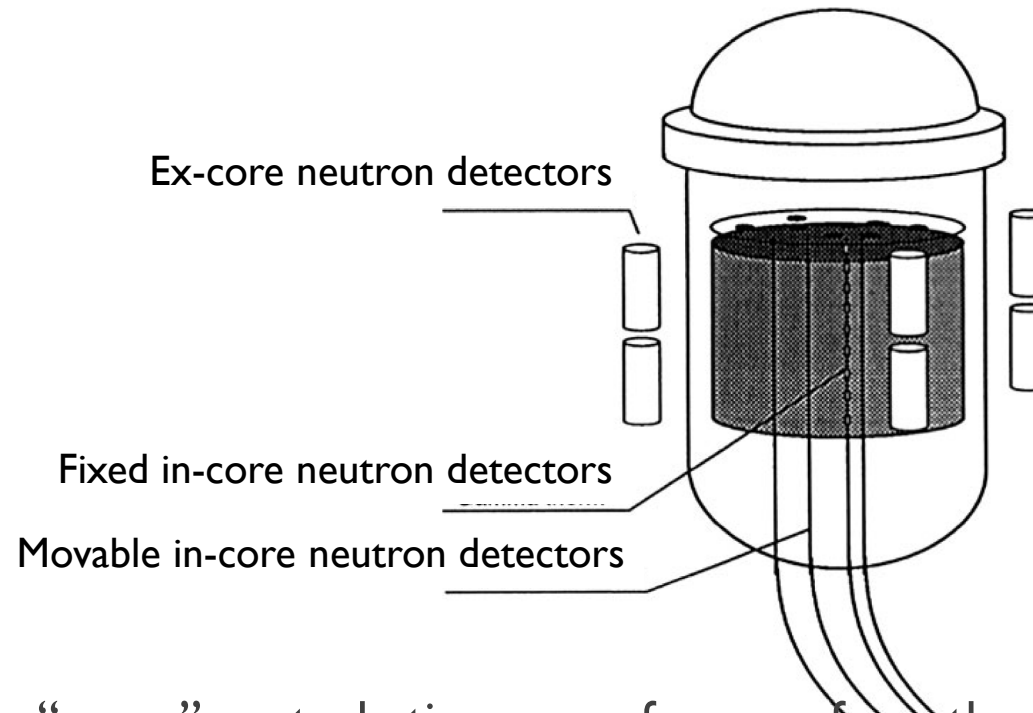
... even if the system is operating at steady-state conditions

- Fluctuations in the neutron density in nuclear reactors can be used for core diagnostics and monitoring



# Introduction and background

- Neutron detectors present both as in-core and ex-core:

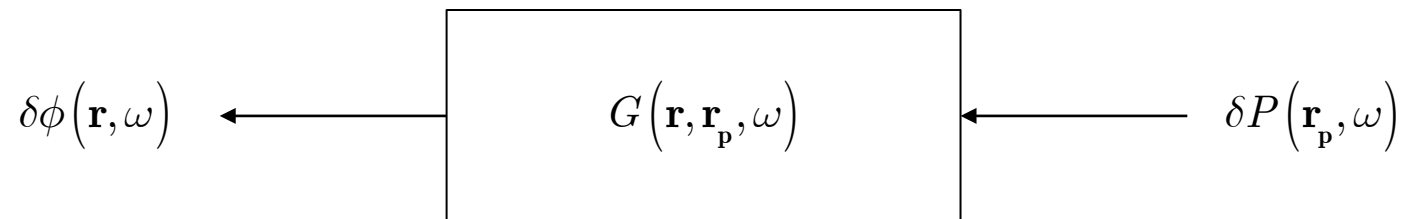


- Advantage: “sense” perturbations even far away from the perturbations
- Disadvantage: western-type reactors do not always contain many in-core neutron detectors



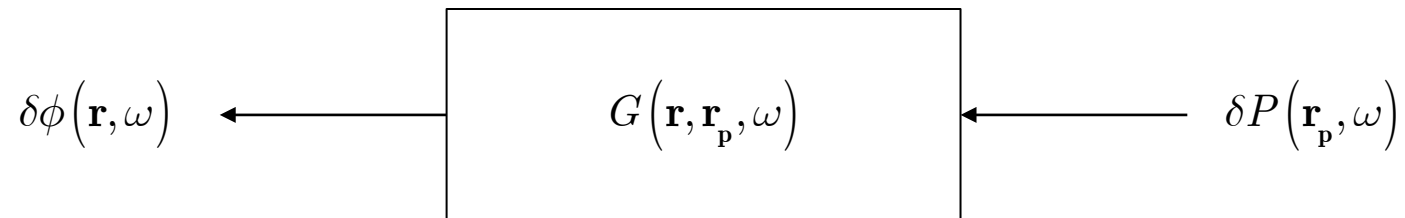
# Introduction and background

- Neutron noise diagnostics requires establishing relationships between neutron detectors and possible perturbations
- The “reactor transfer function”  $G(\mathbf{r}, \mathbf{r}_p, \omega)$  needs to be determined



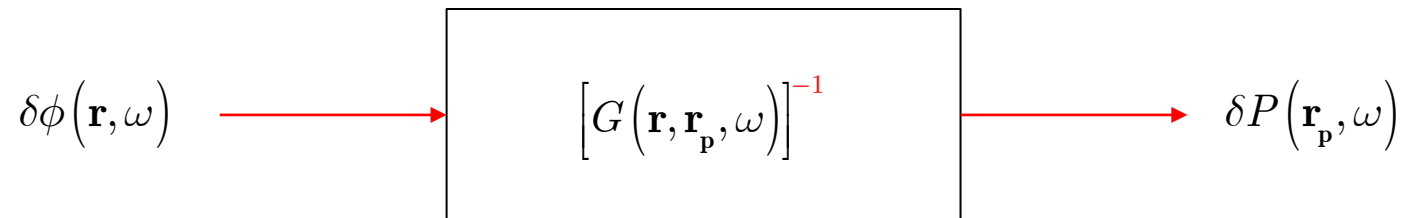
# Introduction and background

- But noise diagnostics requires the inversion of the reactor transfer function  $G(\mathbf{r}, \mathbf{r}_p, \omega)$



# Introduction and background

- But noise diagnostics requires the inversion of the reactor transfer function  $G(\mathbf{r}, \mathbf{r}_p, \omega)$



- Machine learning could be used for that purpose
- Unfolding possible even if very few detectors available (due to the spatial correlations existing between a localized perturbation and its effect throughout the nuclear core)

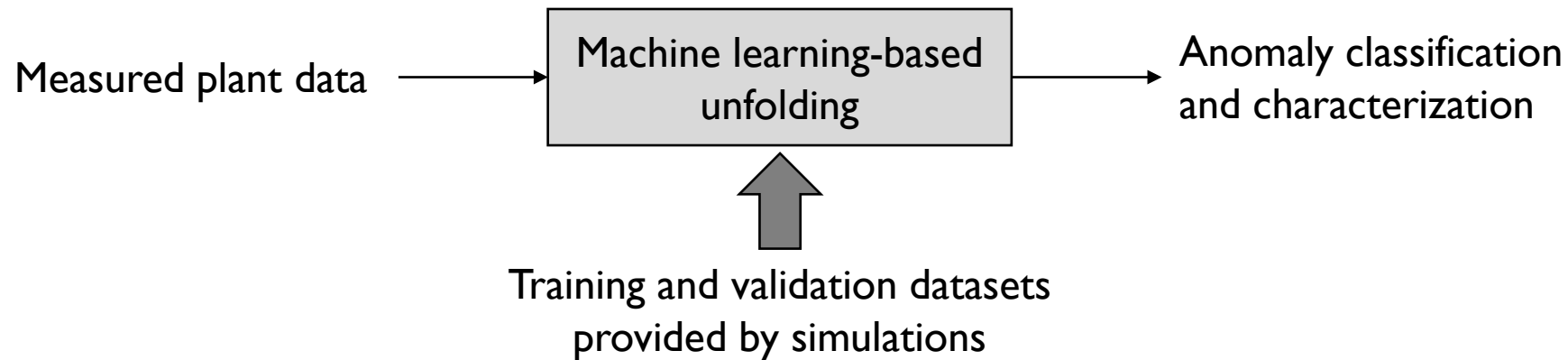


# CORTEX project overview



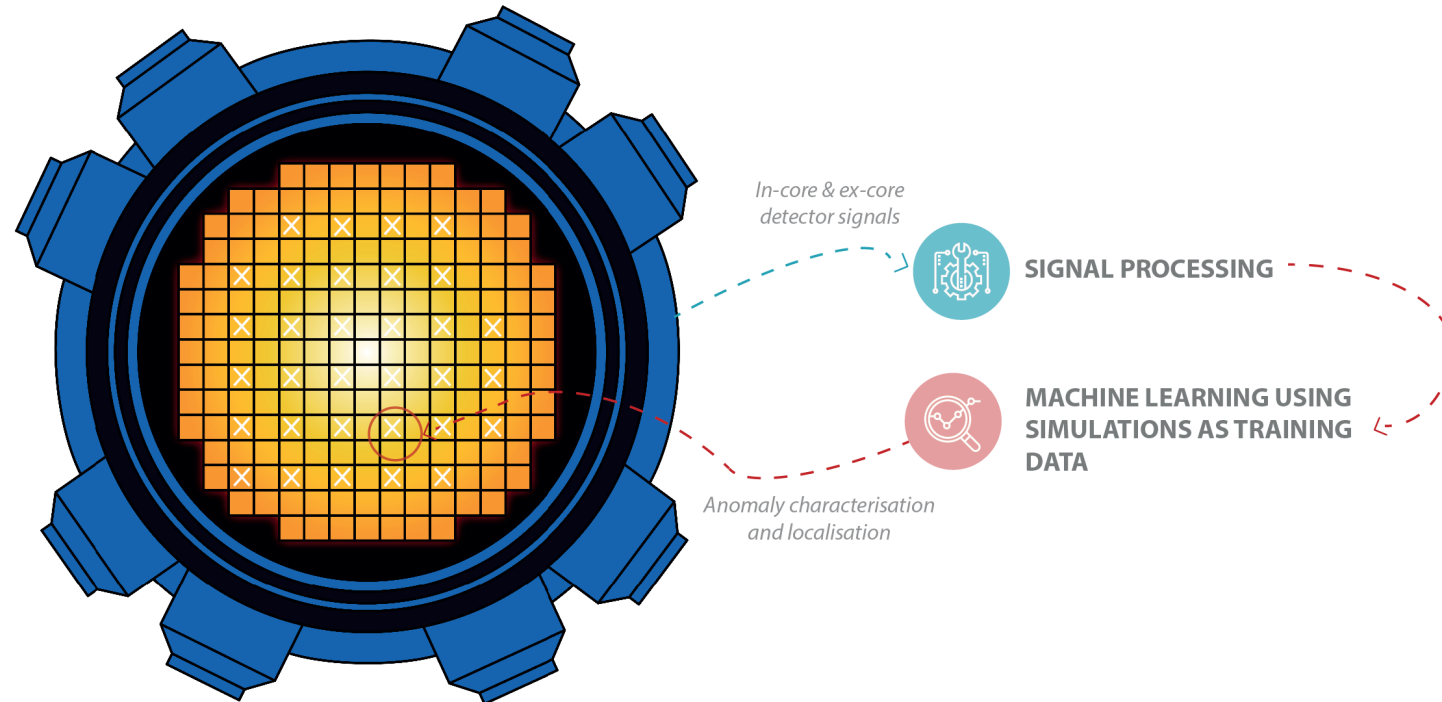
# CORTEX project overview

- Basic principle:
  - Annotated data can only be provided by simulations:



# CORTEX project overview

- 4-year project financed by the European Union (ended in August 2021)
- 18 European organizations + 1 American partner + 1 Japanese partner
- More than 70 researchers involved



More info at:  
[cortex-h2020.eu](http://cortex-h2020.eu)



# Theoretical basis of neutron noise and core diagnostics



# Theoretical basis of neutron noise and core diagnostics

- Modelling of the neutron noise can be done using the neutron transport equation (Boltzmann equation):

$$\begin{aligned} & \frac{1}{v(E)} \frac{\partial}{\partial t} \psi(\mathbf{r}, \boldsymbol{\Omega}, E, t) \\ &= -\boldsymbol{\Omega} \cdot \nabla \psi(\mathbf{r}, \boldsymbol{\Omega}, E, t) - \Sigma_t(\mathbf{r}, E, t) \psi(\mathbf{r}, \boldsymbol{\Omega}, E, t) \\ &+ \int_{(4\pi)} \int_0^\infty \Sigma_s(\mathbf{r}, \boldsymbol{\Omega}' \rightarrow \boldsymbol{\Omega}, E' \rightarrow E, t) \psi(\mathbf{r}, \boldsymbol{\Omega}', E', t) d^2\boldsymbol{\Omega}' dE' \\ &+ \frac{1}{4\pi} \int_{-\infty}^t \int_0^\infty \nu(E') \Sigma_f(\mathbf{r}, E', t') \phi(\mathbf{r}, E', t') \left[ (1 - \beta) \chi^p(E) \delta(t - t') + \sum_{i=1}^{N_d} \chi_i^d(E) \lambda_i \beta_i e^{-\lambda_i(t-t')} \right] dt' dE' \end{aligned}$$

- A model to represent the effect of a given perturbation onto the macroscopic cross-section is required





# Theoretical basis of neutron noise and core diagnostics

- Modelling of the effect of the cross-section perturbations onto the neutron flux can be done in several ways:
  - Low/high order in angle
  - Low/high order in space
  - Low/high order in energy
  - Time- or frequency-domain
  - Deterministic methods or probabilistic methods (Monte Carlo)



# Theoretical basis of neutron noise and core diagnostics

- For diagnostic purposes, one needs to check that the induced neutron noise is significantly different, depending on the type of perturbation and its location
  - Examination of the amplitude and phase of the neutron noise usually allows differentiating the type of perturbation
  - Nevertheless, some more intricate responses can arise in some cases
    - Requires a faithful modelling of the reactor transfer function



# Theoretical basis of neutron noise and core diagnostics

- For the identification of the location of a perturbation, an appreciable deviation from point-kinetics is required
- Induced neutron noise in first-order in the frequency-domain:

$$\delta\phi(\mathbf{r}, \omega) = \delta P(\omega) \phi_0(\mathbf{r}) + \delta\psi(\mathbf{r}, \omega)$$

with

point-kinetic term

$\delta P(\omega)$  fluctuations of the “amplitude factor”

$\delta\psi(\mathbf{r}, \omega)$  fluctuations of the “shape function”

$\phi_0(\mathbf{r})$  static neutron flux



# Theoretical basis of neutron noise and core diagnostics

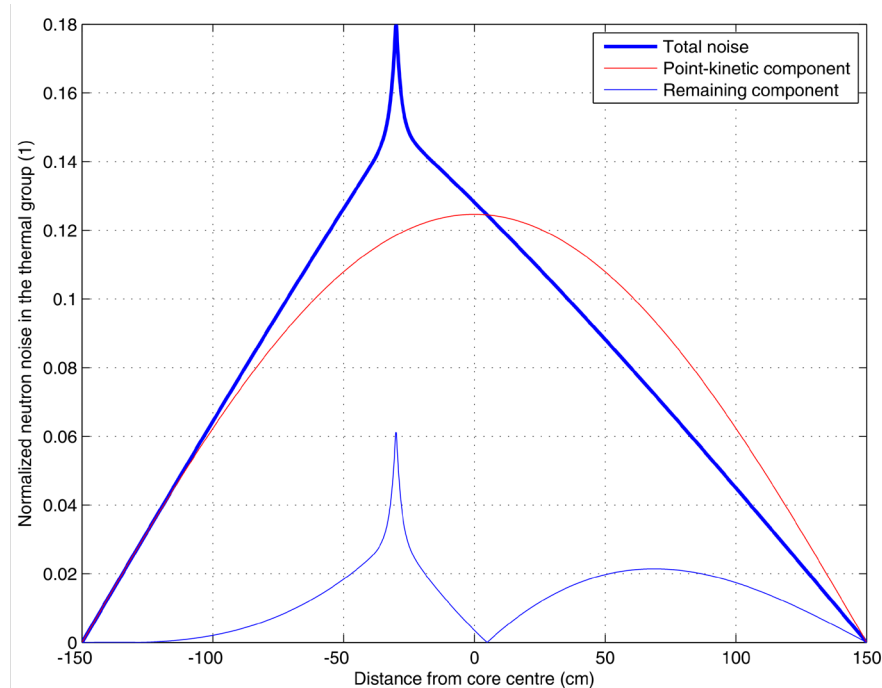


Illustration of the difference between the point-kinetic component and the total induced neutron noise in the frequency domain at 1 Hz, for a perturbation located at -30 cm from the centre of a nuclear core of size 300 cm.



# Application to commercial reactors



# Application to commercial reactors

- Several machine learning-based architectures developed based on:
  - Either time-domain simulations for training/validation
    - De Sousa Ribeiro, F., Calivà, F., Chionis, D., Dokhane, A., Mylonakis, A., Demazière, C., Leontidis, G., Kollias, S. (2018), Towards a deep unified framework for nuclear reactor perturbation analysis. *Proc. IEEE Symposium Series on Computational Intelligence (SSCI 2018)*, Bengaluru, India, November 18 – 21, 2018
    - Durrant, A., Leontidis, G., Kollias, S. (2019), 3D convolutional and recurrent neural networks for reactor perturbation unfolding and anomaly detection. *European Physics Journal Nuclear Sciences and Technologies*, **5**, 20
    - Tasakos, T., Ioannou, G., Verma, V., Alexandridis, G., Dokhane, A., Stafylopatis, A. (2021), Deep learning-based anomaly detection in nuclear reactor cores. *Proc. Int. Conf. Mathematics and Computational Methods Applied to Nuclear Science and Engineering (M&C2021)*, Raleigh, NC, USA, October 3-7, 2021



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    - Durrant, A., Leontidis, G., Kollias, S., Torres, L.A., Montalvo, C., Mylonakis, A., Demazière, C., Vinai, P. (2021), Detection and localisation of multiple in-core perturbations with neutron noise-based self-supervised domain adaptation. *Proc. Int. Conf. Mathematics and Computational Methods Applied to Nuclear Science and Engineering (M&C2021)*, Raleigh, NC, USA, October 3-7, 2021
    - Ioannou G., Tasakos T., Mylonakis A., Alexandridis G., Demazière C., Vinai P., and Stafylopatis A., Feature extraction and identification techniques for the alignment of perturbation simulations with power plant measurements. *Proc. Int. Conf. Mathematics and Computational Methods Applied to Nuclear Science and Engineering (M&C2021)*, Raleigh, NC, USA, October 3-7, 2021





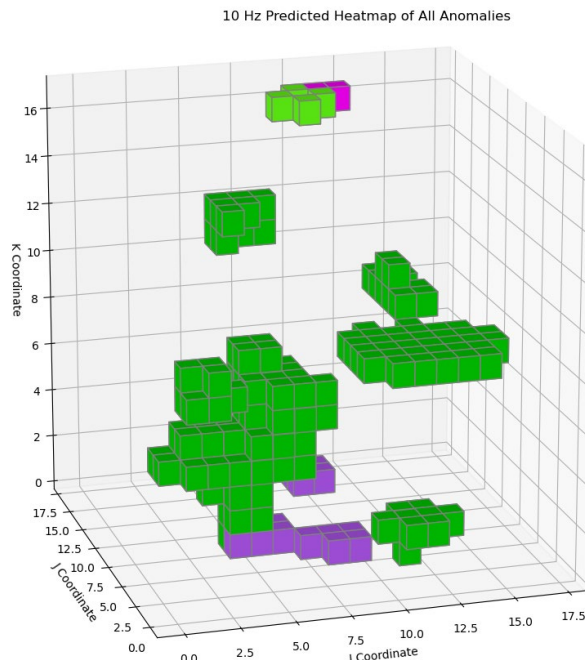
# Application to commercial reactors

- Overall conclusions:
  - Very good unfolding capabilities, both in terms of classification and localization of anomalies
  - Significant enough deviation from point-kinetics
  - Satisfactory results:
    - Even when using very few detectors (but more detectors give better predictions)
    - Even when adding uncorrelated noise
  - More evenly distributed detectors lead to more robust predictions

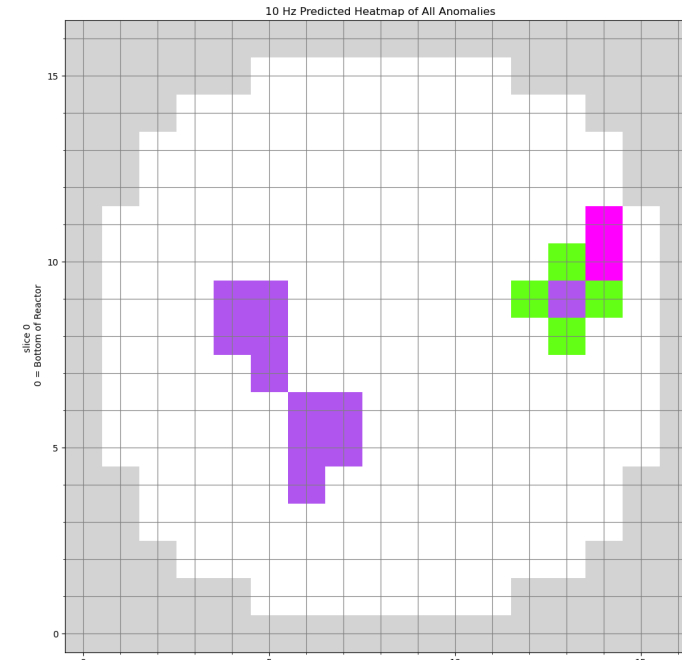


# Application to commercial reactors

- Example of machine learning-based unfolding applied to actual plant data:



Fuel assembly vibrations  
Travelling perturbation  
Absorber of variable strength  
Control rod vibrations



Example of machine learning-based unfolding at 10 Hz in a commercial 4-loop pre-Konvoi PWR

Figure from Durrant, A., Leontidis, G., Kollias, S., Torres, L. A., Montalvo, C., Mylonakis, A., Demazière, C., Vinai, P. (2021), Detection and localisation of multiple in-core perturbations with neutron noise-based self-supervised domain adaptation. Proc. Int. Conf. Mathematics and Computational Methods Applied to Nuclear Science and Engineering (M&C2021), Raleigh, NC, USA, October 3-7, 2021

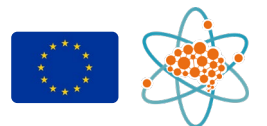


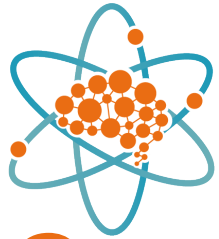
# Conclusions



# Conclusions

- CORTEX project demonstrated that machine-learning based unfolding using annotated simulated data can be used for core monitoring
- Could be used by utilities as a decision-making supportive instrument for plant operation and maintenance





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