

CORTEX Training Course

UP and SA under the Condition of Neutron Flux Oscillation

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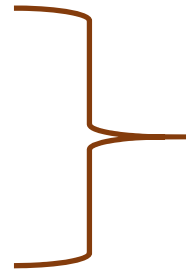
Dec 05, 2019

UP and SA under Neutron Flux Oscillation

Uncertainty Propagation

Initial design/operating parameter #1
Initial design/operating parameter #2
⋮
Initial design/operating parameter #N

$\pm\sigma_1$
 $\pm\sigma_2$
⋮
 $\pm\sigma_N$



Output result

$\pm\sigma_{OUTPUT}$

Sensitivity Analysis

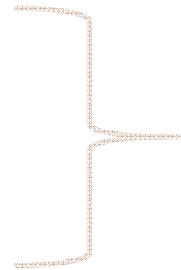


UP and SA under Neutron Flux Oscillation

Uncertainty Propagation

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Output result

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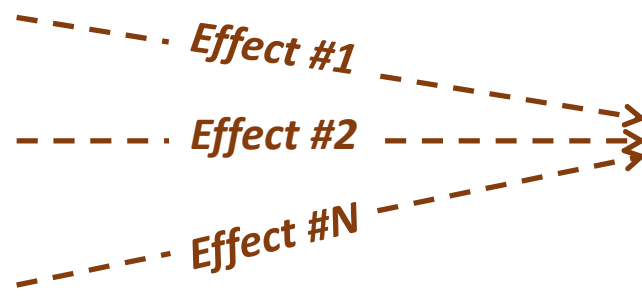
Sensitivity Analysis

Initial design/operating parameter #1

Initial design/operating parameter #2

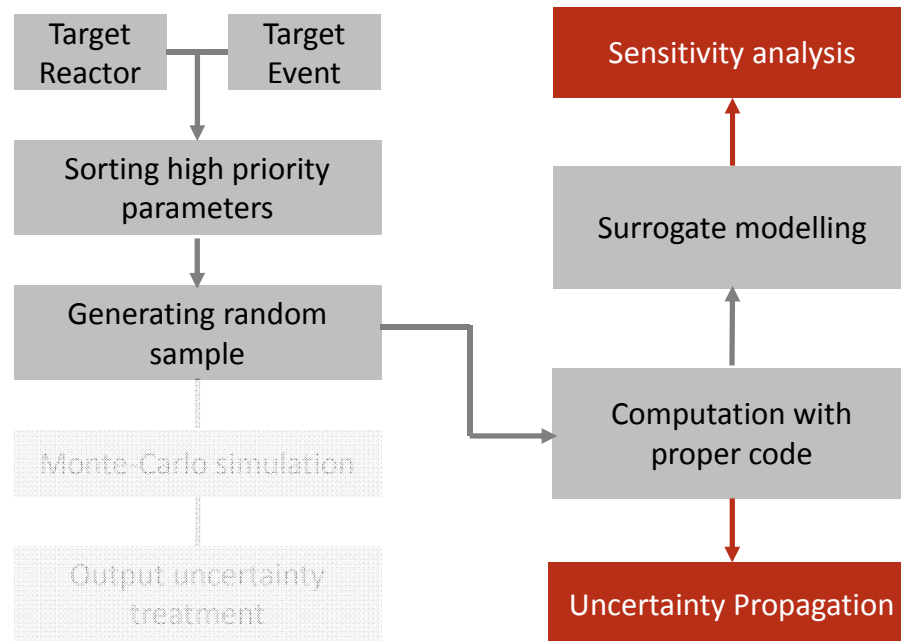
⋮

Initial design/operating parameter #N

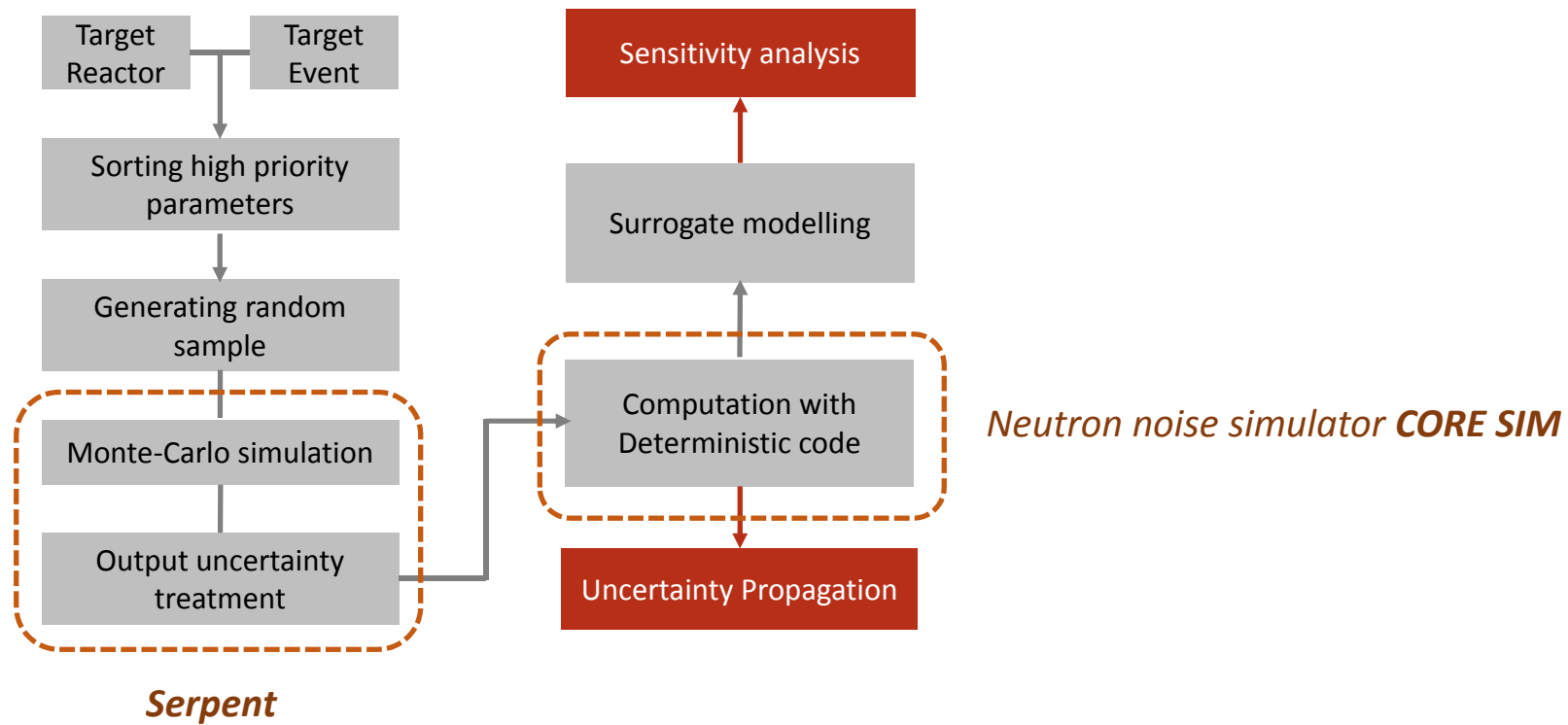


Output behavior

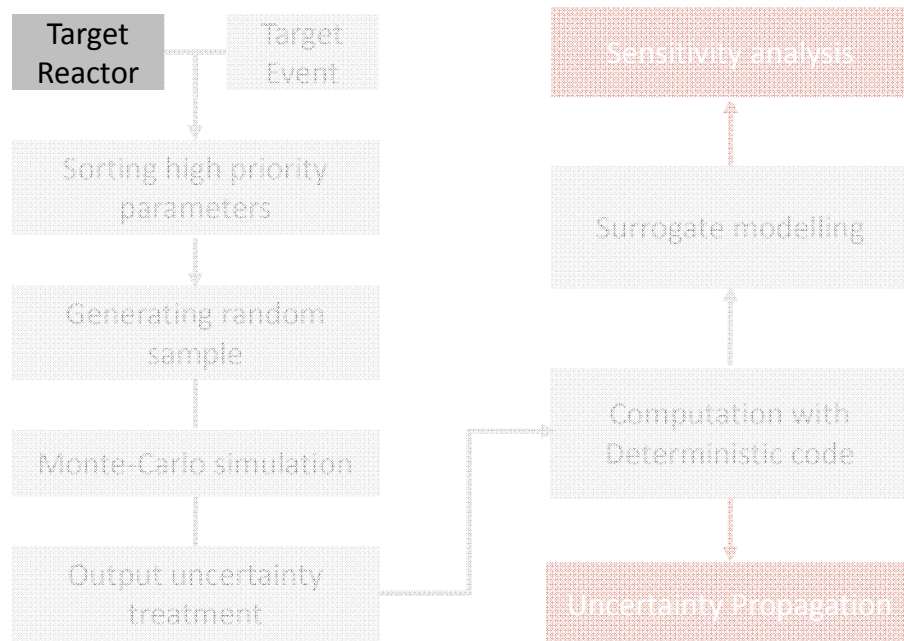
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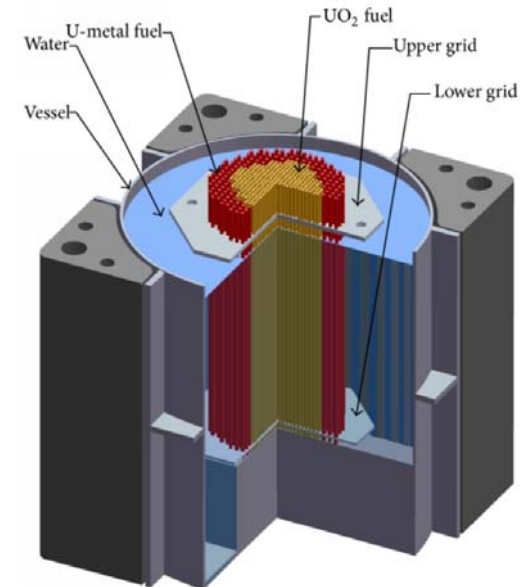
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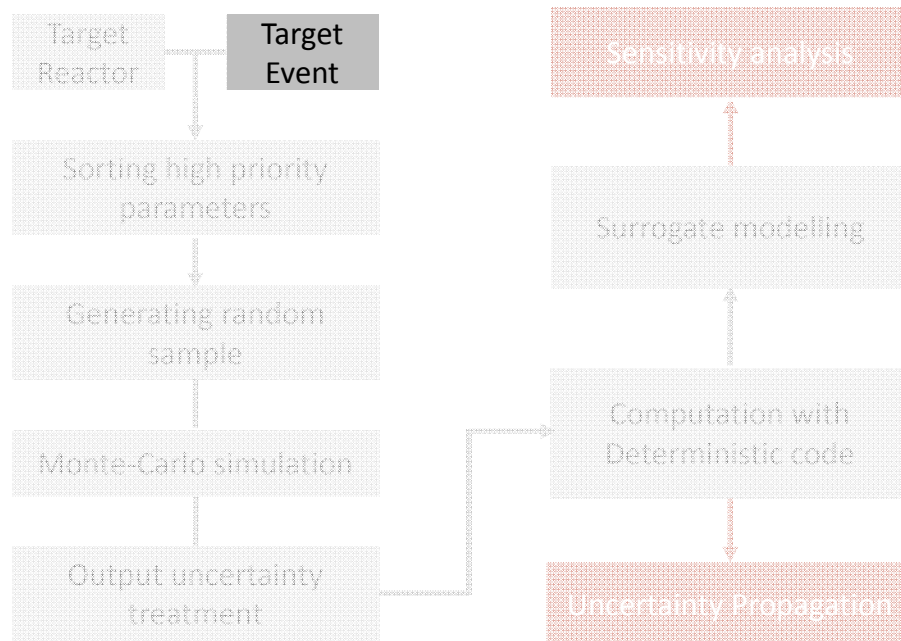


- CROCUS at EPFL
- Zero power reactor ($100W_{max}$)
- 336 UO_2 cells, 176 U_{metal} cells
- Water reflector



Adolfo Rais et al., „Methods and Models for the Coupled Neutronics and Thermal-Hydraulics Analysis of the CROCUS Reactor at EPFL“, *Science and Technology of Nuclear Installations*, Vol 2015, 2015.

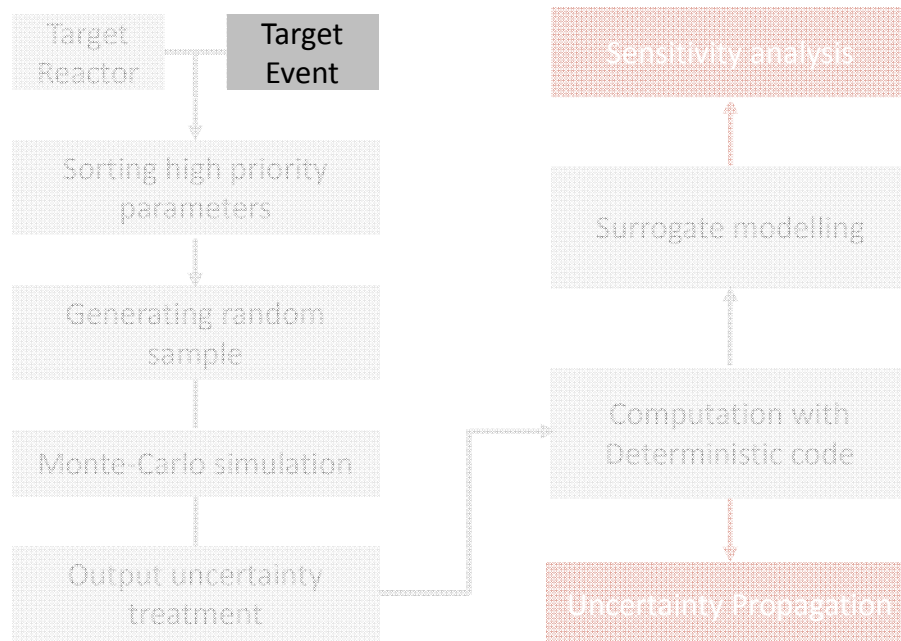
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1	Absorber of variable strength
2	Axially-travelling perturbations
3	Fuel assembly vibrations
4	Control rod vibrations
5	Core barrel vibrations

Different on how to model the input data for noise calculation

UP and SA under Neutron Flux Oscillation



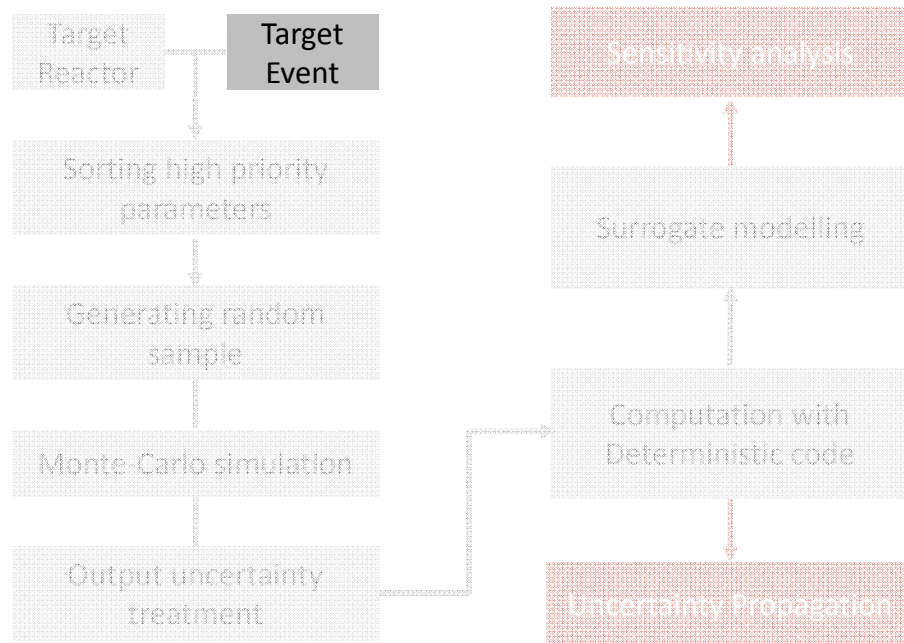
Absorber of variable strength

- *Perturbation of a macroscopic cross-section*
- *Artificial perturbation*
- *Constitutes Green's function*

Axial-travelling perturbation

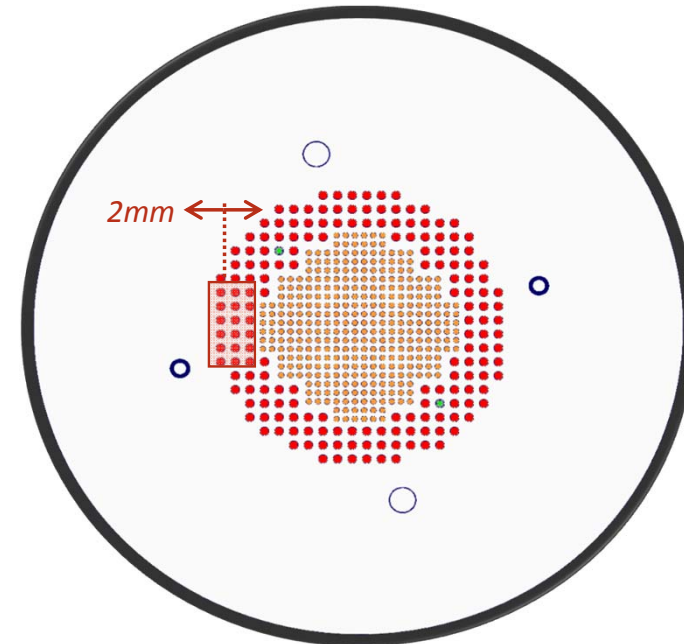
- *Perturbation of the coolant (inside of the core)*
- *Perturbation of the removal cross-section*

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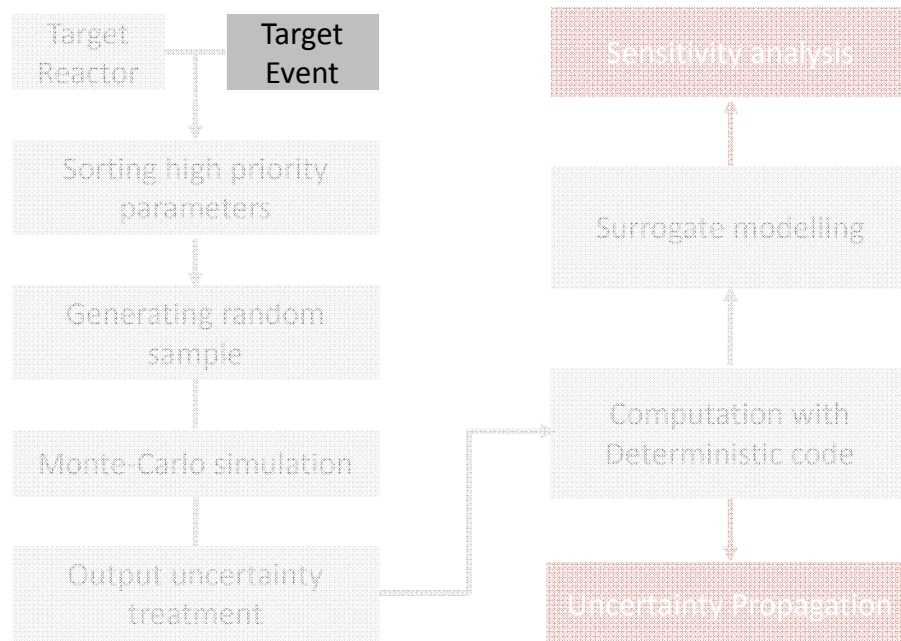


Fuel assembly vibration

- Non-harmonic oscillation of FA (independent from time)
- Test facility in CROCUS reactor (COLIBRI)
-up to 18 fuel rods vibration



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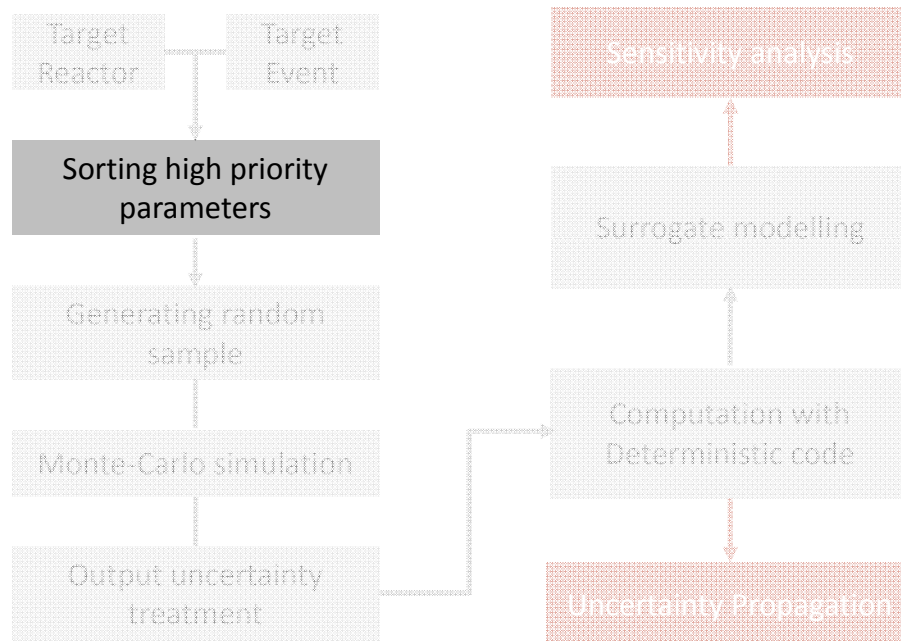
Control rods vibration

- *Vibration of control rod along the z-direction*
- *Perturbation of the thermal absorption cross-section*

Core barrel vibration

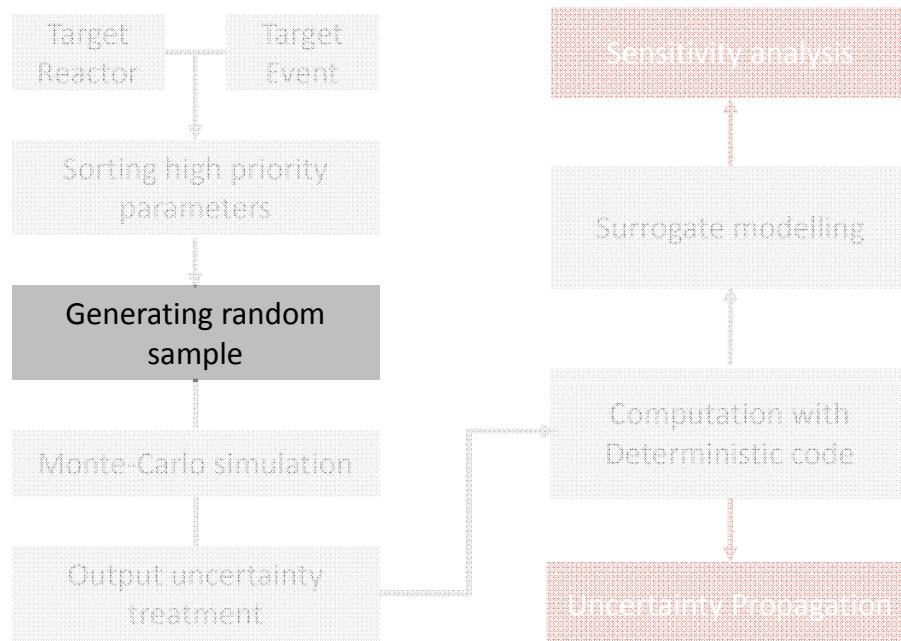
- *Vibration at higher frequency*
- *Results from the interplay between core barrel and RPV*
- *In-phase mode & out-of-phase mode*

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- *Depending on target reactor/ event*
- *Depending on governing theory for output behavior*
- *Expert judgements*

UP and SA under Neutron Flux Oscillation

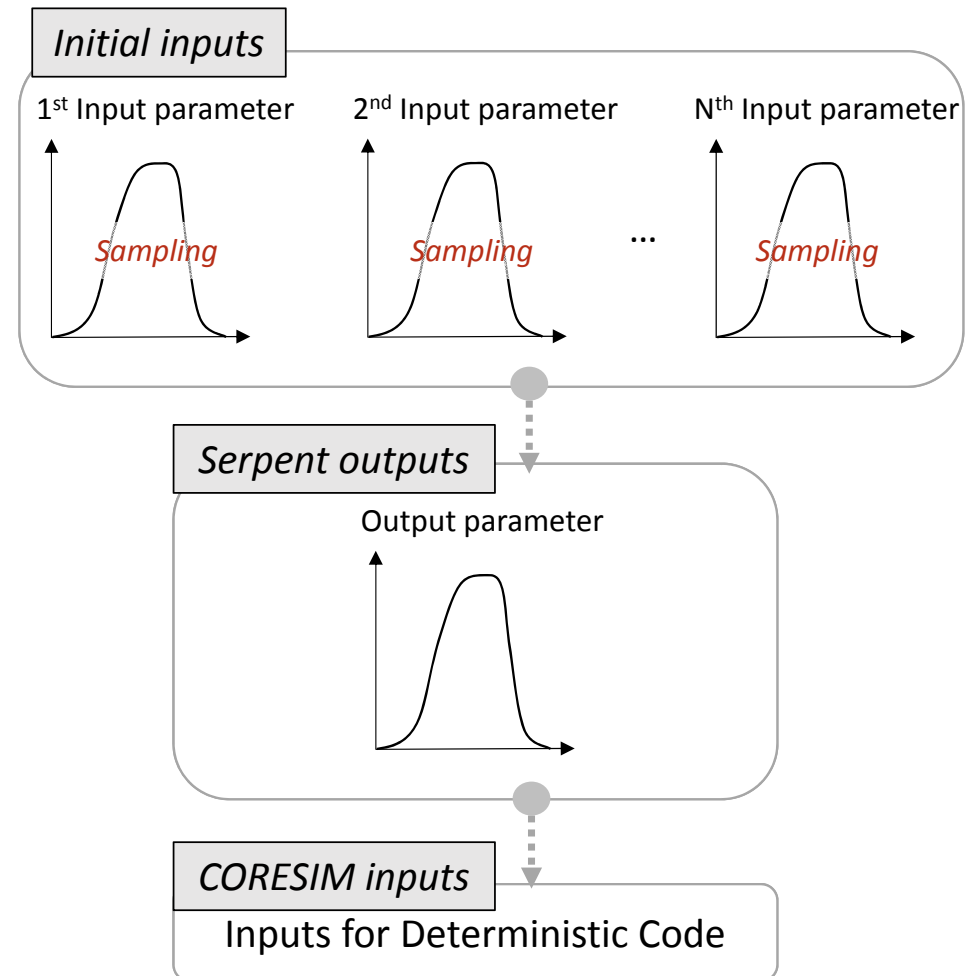
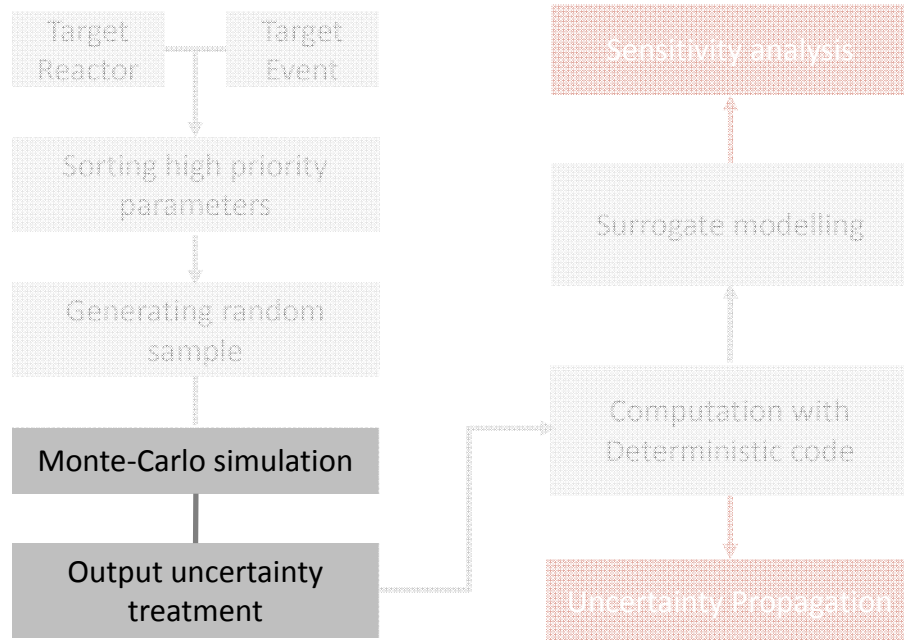


- *Depending on a distribution information*
- *SRS & LHS*

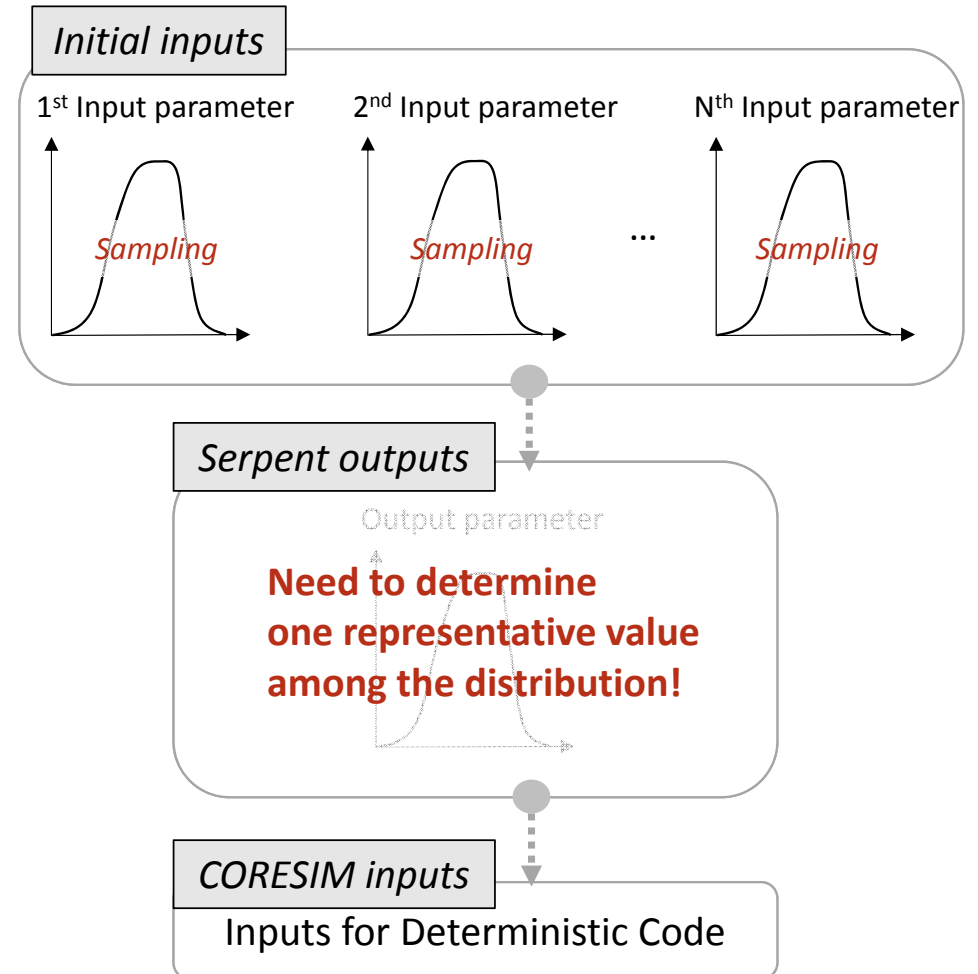
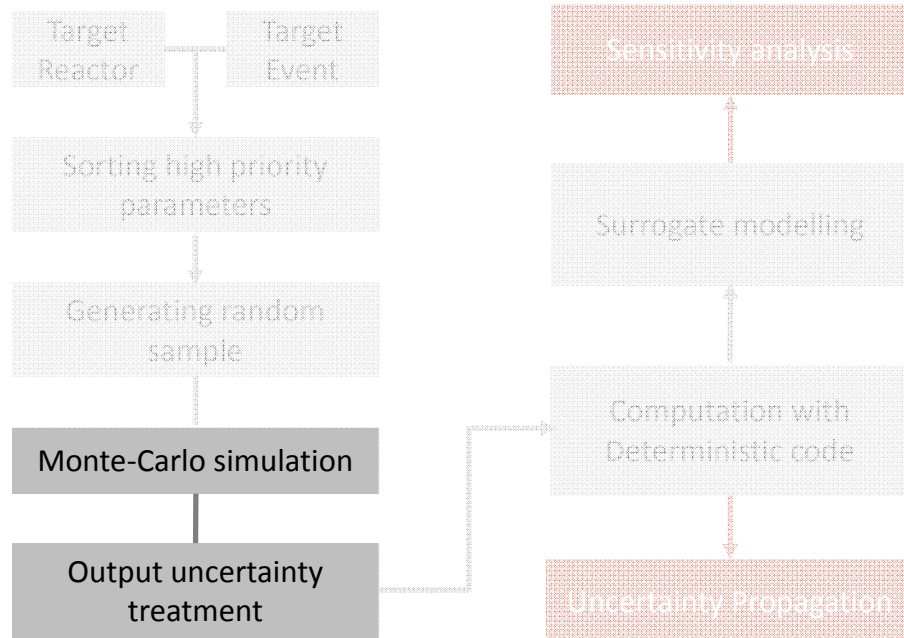
Number of samples?

- *Depending on a purpose of the analysis*
 - Uncertainty propagation (Wilks' formula/ Monte-Carlo)*
 - Sensitivity analysis (Regression based/Correlation based /variance based)*

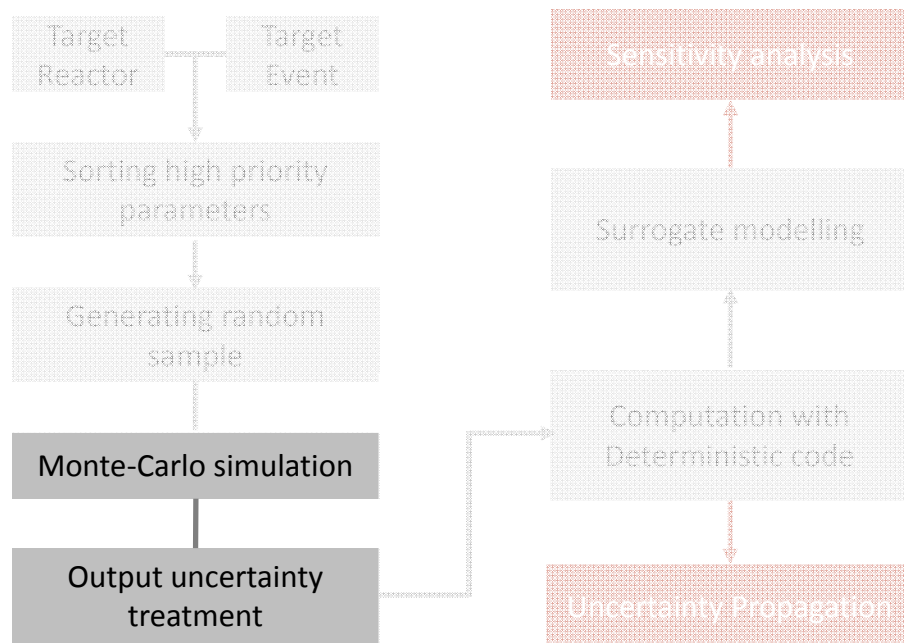
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Resampling SERPENT output data

Target output data :

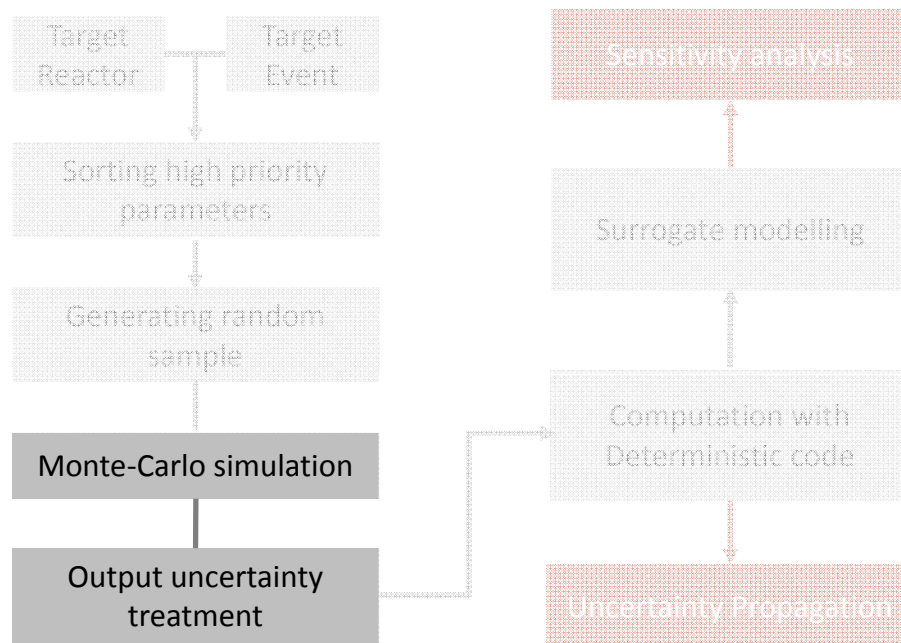
$$\Sigma_a, \Sigma_{rem}, \nu\Sigma_f, D, \beta, \lambda, \delta\Sigma_a, \delta\Sigma_{rem}, \delta\nu\Sigma_f$$

Output data from N input sets:

$$mean_k \pm error_k \quad (1 \leq k \leq N)$$

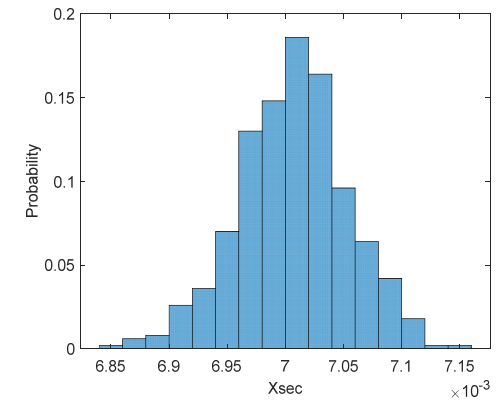
- Modelling normal distribution
- Sampling one value randomly from distribution
- Better to minimize 'error_k'

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Additional consideration on nuclear data unc.

(1) Building a histogram, fitting into normal distribution



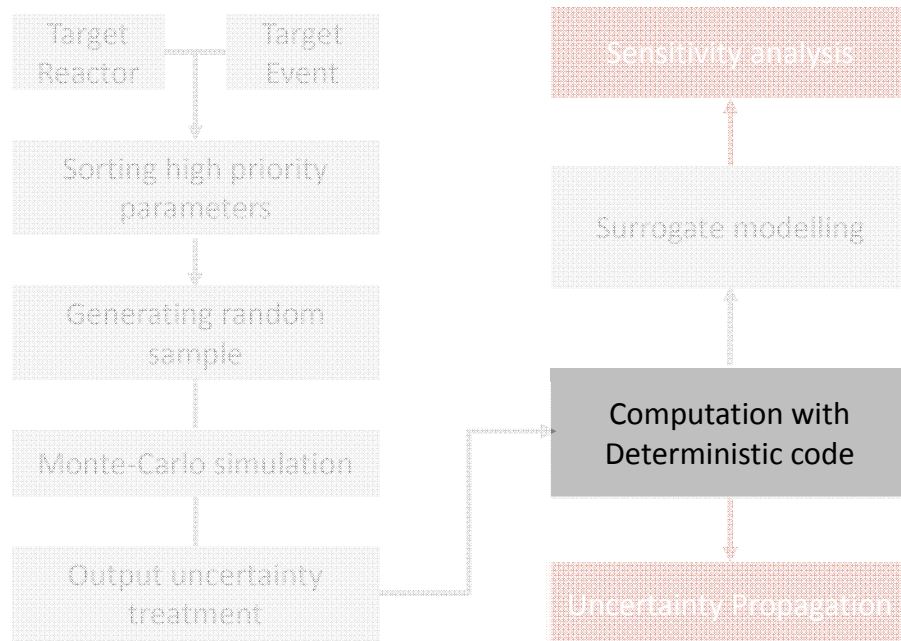
e.g. absorption cross section in UO2 region

(2) Obtaining standard deviation

(3) Combining with XS data (from Serpent) build normal distribution

(4) Extract one value by SRS

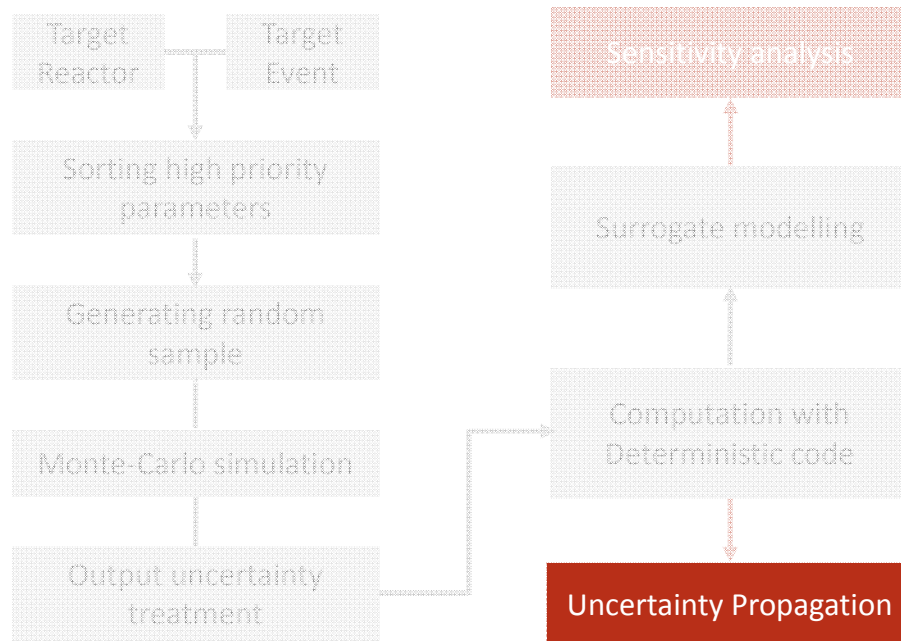
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Final output

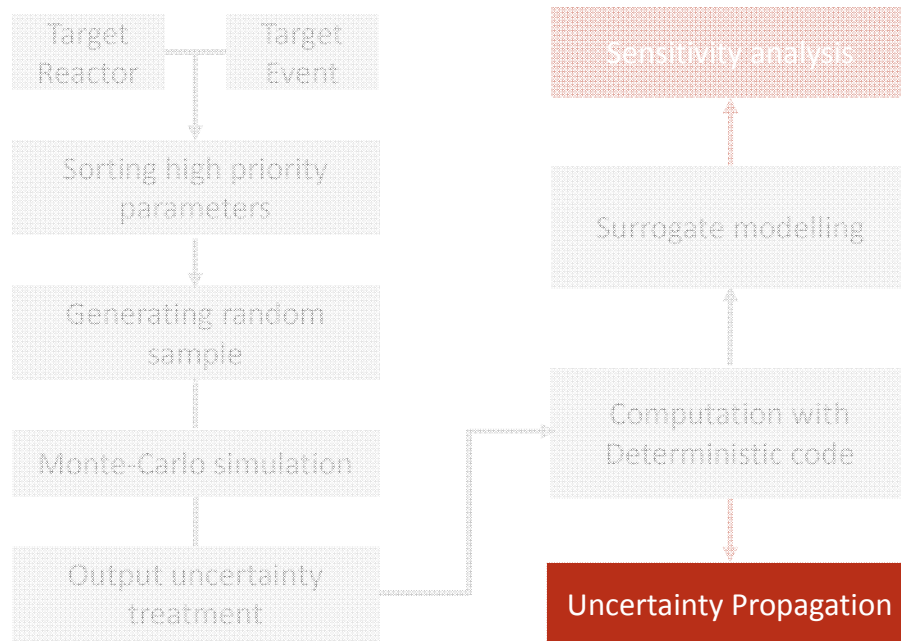
- *Neutron noise data*
 - Extract the value at the location of interest
 - Split the data into magnitude + phase
 - Save the data for further UP & SA

UP and SA under Neutron Flux Oscillation



- **Wilks' formula**
- **Monte-Carlo**

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- **Wilks' formula**

- Nonparametric method**

- Required number of sample sets are dependent on:**

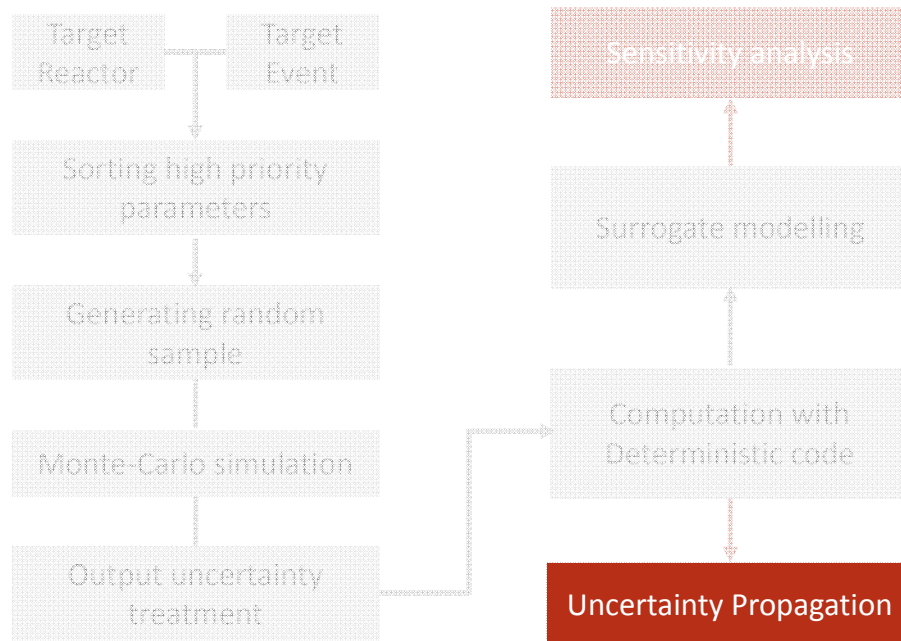
- 1) Tolerance/confidence interval
- 2) One sided limit/two sided limit
- 3) Order of tolerance limit

- Pros and cons**

Pros: easy to use, less number of sample sets

Cons: certain level of conservatism

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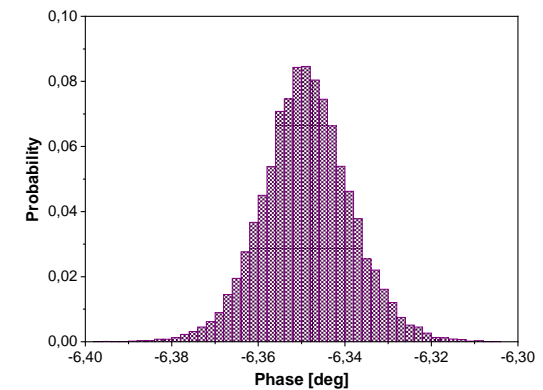
- **Monte-Carlo**

- Pros and cons

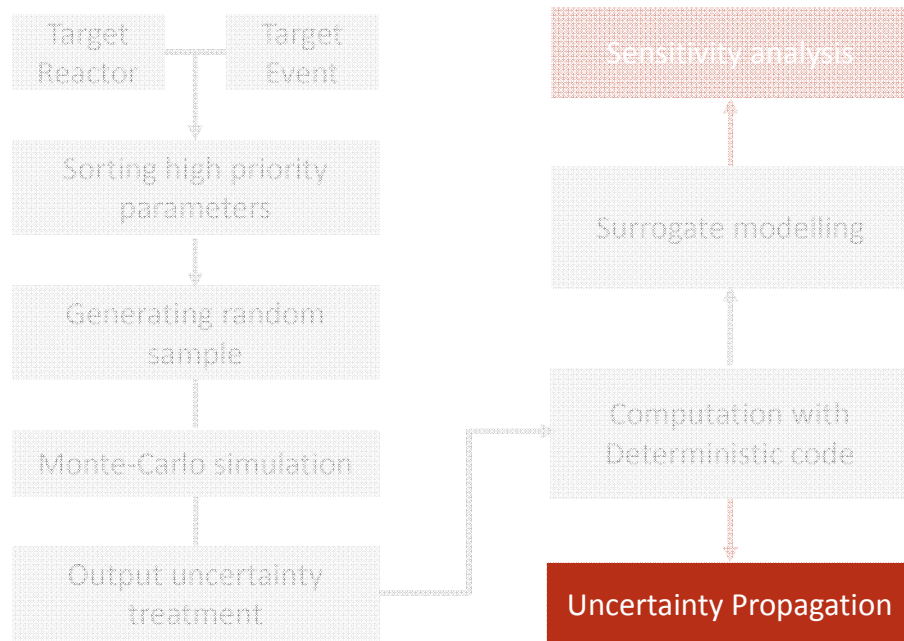
- Pros1* - large number of sample sets → decrease conservatism

- Pros2* - able to yield a full PDF

- Cons* - require a large number of computation (rely on surrogate modelling)



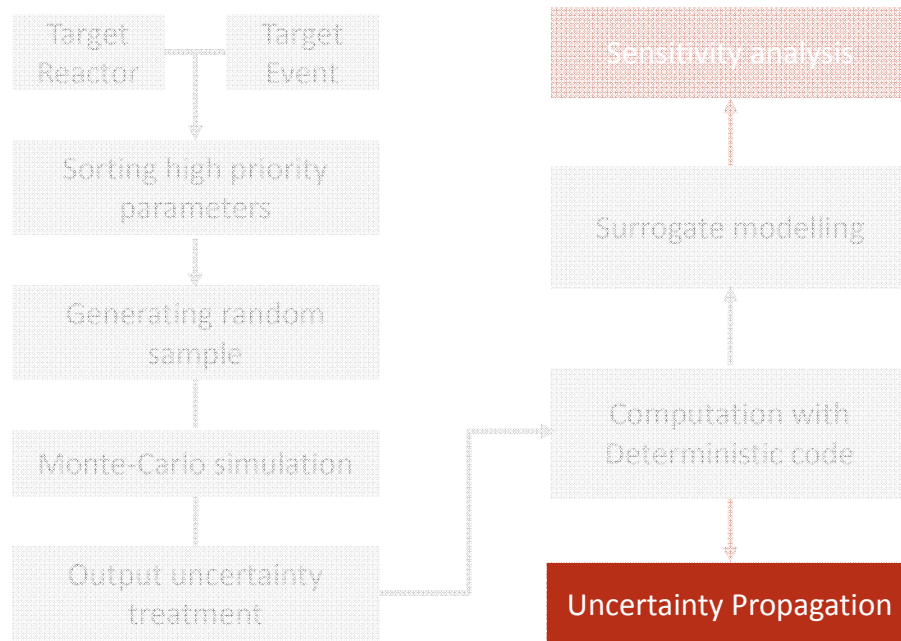
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- **Result comparison between Wilks' approach & Monte-Carlo approach**
-Level of conservatism

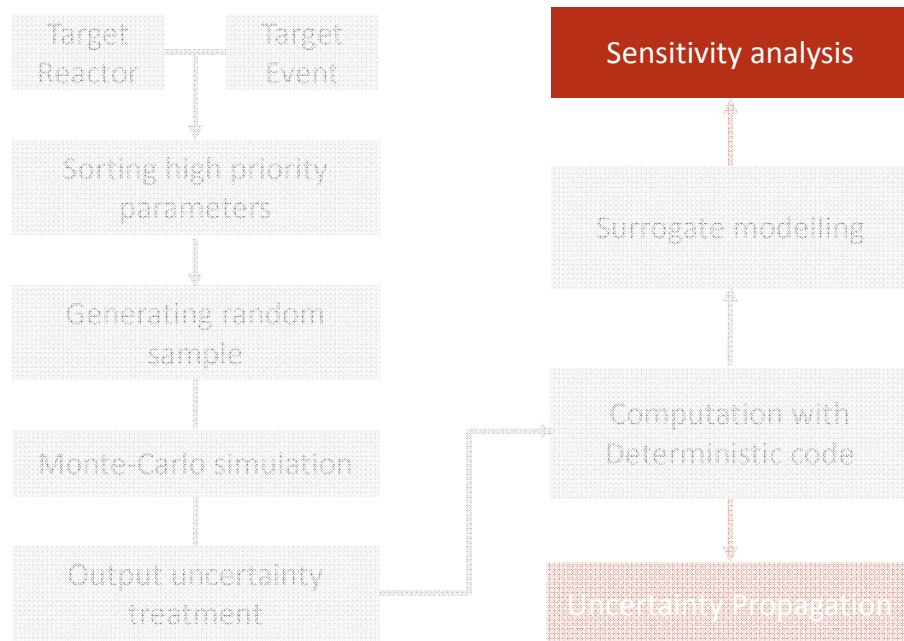


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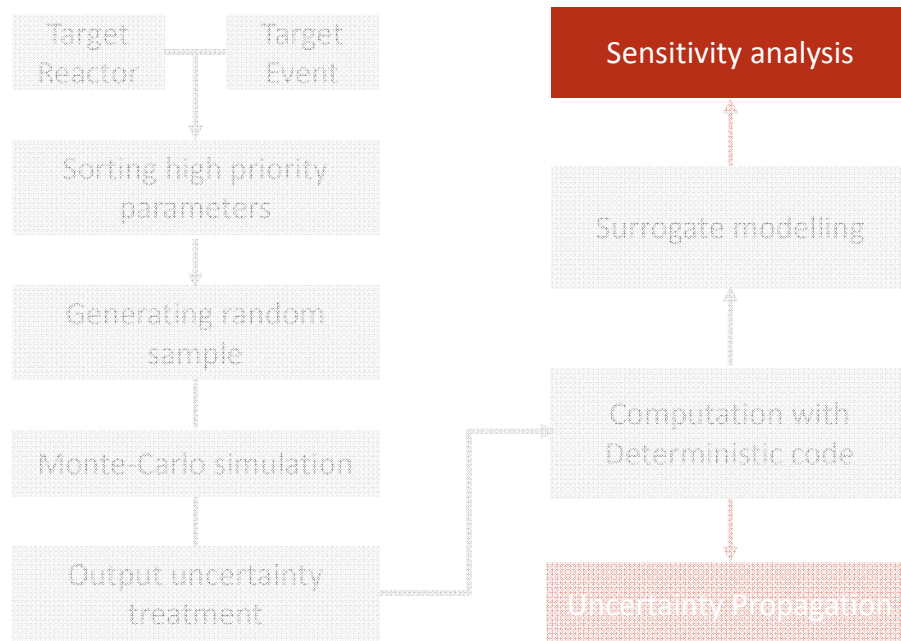
- **The result from UP can be a preview of the result from SA!!**
Larger output uncertainty range
→ More sensitive to the input uncertainty

UP and SA under Neutron Flux Oscillation



- **Regression-based coefficient**
- **Correlation-based coefficient**
- **Variance-based coefficient**

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- **Variance-based coefficient**

- Decomposition of output variance**

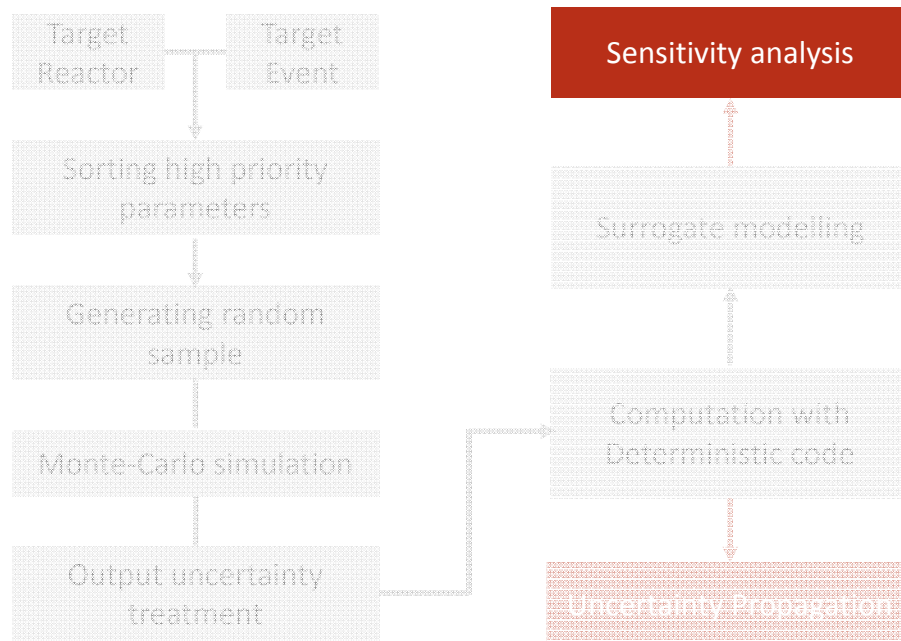
- with main model nonlinear and non-monotonic**

- Pros and cons**

- Pros:** proper for complicated model

- Cons:** costly in terms of the number of computation ($> 10^4$)

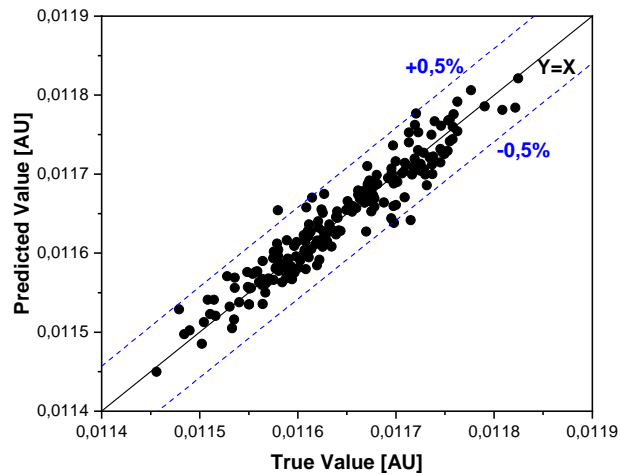
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- **Surrogate modelling**

- The more training sample sets, the higher accuracy
- Training can be failed when there is no/weak correlation between input and output
(when the reactor is small and point-kinetic component is overwhelming, the phase shows less significant value.)

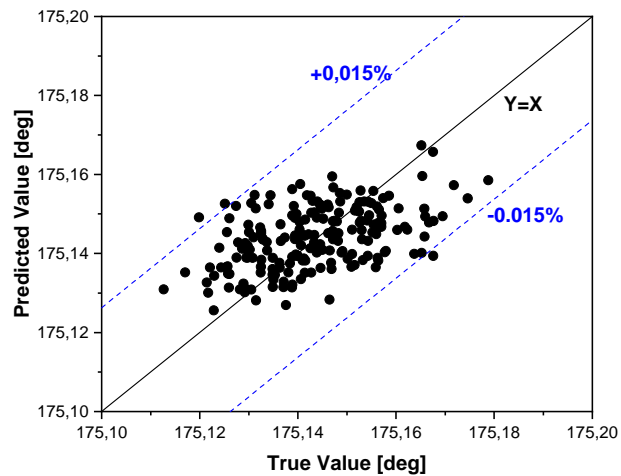
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Good!

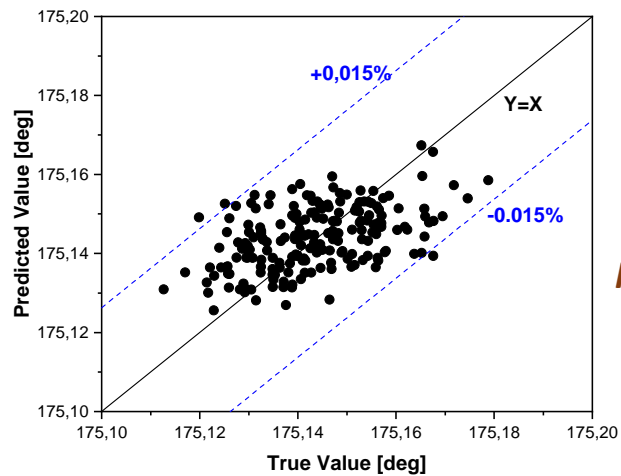
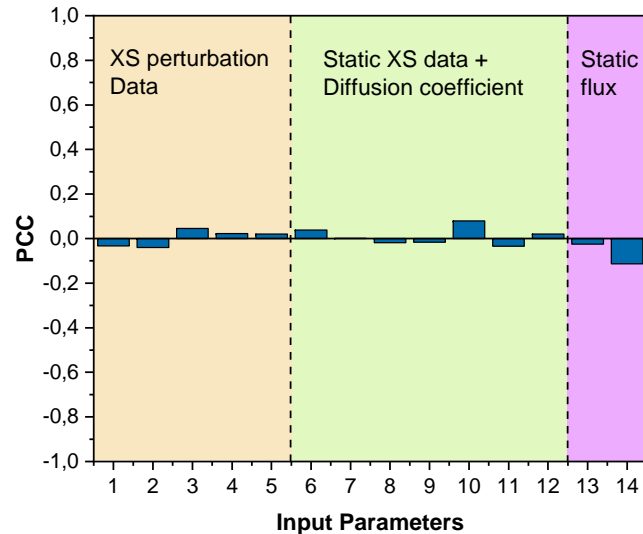
- **Surrogate modelling**

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Fail?!

UP and SA under Neutron Flux Oscillation



- **Surrogate modelling**

- The more training sample sets, the higher accuracy
- Training can be failed when there is no/weak correlation between input and output
(when the reactor is small and point-kinetic component is overwhelming, the phase shows less significant value.)

No strong correlation with input parameters!